



E A O ticks = printed in that board's formulae booklet (Edexcel 9MA0 · AQA 7357 · OCR A H240). No tick: learn it.

Algebra & functions

- ☐☐☐ Quadratic formula:
 $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
- ☐☐☐ Discriminant $b^2 - 4ac$: > 0 two real roots, $= 0$ one repeated root, < 0 no real roots
- ☐☐☐ Completing the square:
 $ax^2 + bx + c = a\left(x + \frac{b}{2a}\right)^2 + c - \frac{b^2}{4a}$
- ☐☐☐ Indices: $a^m a^n = a^{m+n}$, $(a^m)^n = a^{mn}$, $a^{-n} = \frac{1}{a^n}$, $a^{\frac{m}{n}} = \sqrt[n]{a^m}$
- ☐☐☐ Surds: $\sqrt{ab} = \sqrt{a}\sqrt{b}$, $\frac{1}{\sqrt{a}+\sqrt{b}} = \frac{\sqrt{a}-\sqrt{b}}{a-b}$
- ☐☐☐ Factor theorem:
 $f(a) = 0 \iff (x - a) \text{ is a factor}$
- ☐☐☐ Partial fractions:
 $\frac{px+q}{(x-a)(x-b)} = \frac{A}{x-a} + \frac{B}{x-b}$, $\frac{1}{(x-a)^2(x-b)} = \frac{A}{x-a} + \frac{B}{(x-a)^2} + \frac{C}{x-b}$
- ☐☐☐ Modulus; composite; inverse:
 $|x| < a \iff -a < x < a$;
 $fg(x) = f(g(x))$; $f^{-1}(x) = x$
- ☐☐☐ Transformations: $f(x) + a$ up a ;
 $f(x + a)$ left a ; $af(x)$ vertical $\times a$;
 $f(ax)$ horizontal $\times \frac{1}{a}$

Coordinate geometry

- ☐☐☐ Line; gradient:
 $y - y_1 = m(x - x_1)$, $m = \frac{y_2 - y_1}{x_2 - x_1}$
- ☐☐☐ Perpendicular gradients:
 $m_1 m_2 = -1$
- ☐☐☐ Midpoint; distance:
 $\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$,
 $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$
- ☐☐☐ Circle, centre (a, b) , radius r :
 $(x - a)^2 + (y - b)^2 = r^2$
- ☐☐☐ Circles: tangent $\perp$ radius;
angle in a semicircle is 90° ;
perpendicular from centre bisects a chord
- ☐☐☐ Parametric $\rightarrow$ Cartesian:
eliminate t , e.g. with $\sin^2 t + \cos^2 t = 1$

Sequences & series

- ☐☐☐ Arithmetic n th term:
 $u_n = a + (n - 1)d$
- ☐☐☐ Arithmetic series:
 $S_n = \frac{1}{2}n(a + l) = \frac{1}{2}n[2a + (n - 1)d]$
- ☐☐☐ Geometric n th term:
 $u_n = ar^{n-1}$
- ☐☐☐ Geometric series:
 $S_n = \frac{a(1-r^n)}{1-r}$, $S_\infty = \frac{a}{1-r}$ ($|r| < 1$)
- ☐☐☐ Binomial, $n \in \mathbb{N}$:
 $(a + b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + b^n$
- ☐☐☐ Binomial coefficient:
 $\binom{n}{r} = {}^nC_r = \frac{n!}{r!(n-r)!}$
- ☐☐☐ Binomial, $|x| < 1$, $n \in \mathbb{Q}$:
 $(1 + x)^n = 1 + nx + \frac{n(n-1)}{1 \times 2}x^2 + \dots$
- ☐☐☐ $(a + bx)^n = a^n(1 + \frac{b}{a}x)^n$, valid for $|x| < \frac{a}{b}$
- ☐☐☐ Sigma; recurrence:
 $\sum_{r=1}^n r = \frac{1}{2}n(n + 1)$; $u_{n+1} = f(u_n)$

Exponentials & logarithms

- ☐☐☐ Definition:
 $a^x = b \iff x = \log_a b$
- ☐☐☐ Laws:
 $\log_a xy = \log_a x + \log_a y$,
 $\log_a \frac{x}{y} = \log_a x - \log_a y$,
 $\log_a x^k = k \log_a x$
- ☐☐☐ Change of base:
 $\log_a x = \frac{\log_b x}{\log_b a}$
- ☐☐☐ Exponential form: $a^x = e^{x \ln a}$
- ☐☐☐ Inverses: $e^{\ln x} = x$, $\ln e^x = x$
- ☐☐☐ Linearising: $y = ax^n \Rightarrow \log y = \log a + n \log x$; $y = kb^x \Rightarrow \log y = \log k + x \log b$

Trigonometry

- ☐☐☐ Sine rule; cosine rule:
 $\frac{a}{\sin A} = \frac{b}{\sin B}$, $a^2 = b^2 + c^2 - 2bc \cos A$
- ☐☐☐ Area; arc; sector (radians):
 $\frac{1}{2}ab \sin C$; $s = r\theta$; $A = \frac{1}{2}r^2\theta$
- ☐☐☐ Identities: $\tan \theta = \frac{\sin \theta}{\cos \theta}$,
 $\sin^2 \theta + \cos^2 \theta = 1$
- ☐☐☐ Reciprocal:
 $\sec^2 \theta = 1 + \tan^2 \theta$,
 $\operatorname{cosec}^2 \theta = 1 + \cot^2 \theta$
- ☐☐☐ Double angle:
 $\sin 2A = 2 \sin A \cos A$,
 $\cos 2A = \cos^2 A - \sin^2 A = 2 \cos^2 A - 1 = 1 - 2 \sin^2 A$
- ☐☐☐ Double angle (tan):
 $\tan 2A = \frac{2 \tan A}{1 - \tan^2 A}$
- ☐☐☐ Compound sin:
 $\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$
- ☐☐☐ Compound cos:
 $\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$
- ☐☐☐ Compound tan:
 $\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$
- ☐☐☐ Harmonic form, $R > 0$:
 $a \sin \theta + b \cos \theta = R \sin(\theta + \alpha)$,
 $R = \sqrt{a^2 + b^2}$, $\tan \alpha = \frac{b}{a}$
- ☐☐☐ Small angles (radians):
 $\sin \theta \approx \theta$, $\cos \theta \approx 1 - \frac{\theta^2}{2}$, $\tan \theta \approx \theta$
- ☐☐☐ Exact values: $\sin 30^\circ = \frac{1}{2}$,
 $\sin 45^\circ = \frac{\sqrt{2}}{2}$, $\sin 60^\circ = \frac{\sqrt{3}}{2}$,
 $\tan 30^\circ = \frac{1}{\sqrt{3}}$, $\tan 60^\circ = \sqrt{3}$
- ☐☐☐ Inverse trig ranges:
 $\arcsin \in [-\frac{\pi}{2}, \frac{\pi}{2}]$, $\arccos \in [0, \pi]$,
 $\arctan \in (-\frac{\pi}{2}, \frac{\pi}{2})$
- ☐☐☐ Radians: $\pi \text{ rad} = 180^\circ$

Differentiation

- ☐☐☐ First principles:
 $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$
- ☐☐☐ Standard: $(x^n)' = nx^{n-1}$,
 $(e^{kx})' = ke^{kx}$, $(\ln x)' = \frac{1}{x}$,
 $(\sin kx)' = k \cos kx$,
 $(\cos kx)' = -k \sin kx$
- ☐☐☐ Exponential base a :
 $(a^{kx})' = ka^{kx} \ln a$

- ☐☐☐ Trig: $(\tan kx)' = k \sec^2 kx$,
 $(\sec kx)' = k \sec kx \tan kx$,
 $(\cot kx)' = -k \operatorname{cosec}^2 kx$,
 $(\operatorname{cosec} kx)' = -k \operatorname{cosec} kx \cot kx$
- ☐☐☐ Product; chain:
 $(uv)' = uv' + vu'$, $\frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx}$
- ☐☐☐ Quotient: $\frac{d}{dx} \left(\frac{f}{g} \right) = \frac{f'g - fg'}{g^2}$
- ☐☐☐ Inverse; parametric:
 $\frac{dy}{dx} = \frac{1}{dx/dy}$; $\frac{dy}{dx} = \frac{dy/dt}{dx/dt}$
- ☐☐☐ Implicit: $\frac{d}{dx} f(y) = f'(y) \frac{dy}{dx}$,
 $\frac{d}{dx}(xy) = x \frac{dy}{dx} + y$
- ☐☐☐ Stationary: $f' = 0$; max if $f'' < 0$, min if $f'' > 0$. Convex $f'' > 0$, concave $f'' < 0$; inflection: f'' changes sign
- ☐☐☐ Tangent; normal:
 $y - y_1 = f'(x_1)(x - x_1)$;
 $m_n = -\frac{1}{f'(x_1)}$

Integration

- ☐☐☐ Standard: $\int x^n dx = \frac{x^{n+1}}{n+1} + c$,
 $\int \frac{1}{x} dx = \ln |x| + c$,
 $\int e^{kx} dx = \frac{1}{k} e^{kx} + c$
- ☐☐☐ Trig:
 $\int \cos kx dx = \frac{1}{k} \sin kx + c$,
 $\int \sin kx dx = -\frac{1}{k} \cos kx + c$
- ☐☐☐ More trig:
 $\int \sec^2 kx dx = \frac{1}{k} \tan kx + c$,
 $\int \tan kx dx = \frac{1}{k} \ln |\sec kx| + c$,
 $\int \cot kx dx = \frac{1}{k} \ln |\sin kx| + c$
- ☐☐☐ Reverse chain: $\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + c$,
 $\int f'(x)[f(x)]^n dx = \frac{[f(x)]^{n+1}}{n+1} + c$
- ☐☐☐ Linear inside:
 $\int f(ax + b) dx = \frac{1}{a} F(ax + b) + c$
- ☐☐☐ By parts: $\int u \frac{dv}{dx} dx = uv - \int v \frac{du}{dx} dx$
- ☐☐☐ Substitution: $u = g(x)$, replace dx by $\frac{du}{g'(x)}$, change the limits
- ☐☐☐ Area: $\int_a^b y dx$;
between curves $\int_a^b (y_{\text{top}} - y_{\text{bottom}}) dx$;
parametric $\int y \frac{dx}{dt} dt$
- ☐☐☐ Identities to integrate:
 $\sin^2 x = \frac{1}{2}(1 - \cos 2x)$,
 $\cos^2 x = \frac{1}{2}(1 + \cos 2x)$
- ☐☐☐ Separable DE: $\frac{dy}{dx} = f(x)g(y)$
 $\Rightarrow \int \frac{dy}{g(y)} = \int f(x) dx$

Numerical methods & vectors

- ☐☐☐ Trapezium rule, $h = \frac{b-a}{n}$:
 $\int_a^b y dx \approx \frac{1}{2}h\{y_0 + y_n\} + 2(y_1 + \dots + y_{n-1})$
- ☐☐☐ Newton-Raphson:
 $x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$
- ☐☐☐ Sign change: continuous f with $f(a)f(b) < 0$ has a root in (a, b) . Iteration $x_{n+1} = g(x_n)$: staircase/cobweb
- ☐☐☐ Magnitude; unit vector:
 $|\mathbf{x}\mathbf{i} + y\mathbf{j} + z\mathbf{k}| = \sqrt{x^2 + y^2 + z^2}$,
 $\hat{\mathbf{a}} = \frac{\mathbf{a}}{|\mathbf{a}|}$

- ☐☐☐ $\overrightarrow{AB}$; distance AB : $\mathbf{b} - \mathbf{a}$;
 $|\mathbf{b} - \mathbf{a}| = \sqrt{\Delta x^2 + \Delta y^2 + \Delta z^2}$

Mechanics

- ☐☐☐ Constant acceleration:
 $v = u + at$, $s = ut + \frac{1}{2}at^2$,
 $s = vt - \frac{1}{2}at^2$, $s = \frac{1}{2}(u + v)t$,
 $v^2 = u^2 + 2as$
- ☐☐☐ ... in vectors: $\mathbf{v} = \mathbf{u} + \mathbf{at}$,
 $\mathbf{r} = \mathbf{ut} + \frac{1}{2}\mathbf{at}^2$
- ☐☐☐ Variable acceleration: $v = \frac{dx}{dt}$,
 $a = \frac{dv}{dt} = \frac{d^2x}{dt^2}$, $\mathbf{r} = \int \mathbf{v} dt$, $\mathbf{v} = \int \mathbf{a} dt$
- ☐☐☐ Forces: $\mathbf{F} = m\mathbf{a}$, $\mathbf{W} = m\mathbf{g}$,
 $F \leq \mu R$ (limiting: $F = \mu R$)
- ☐☐☐ Moments: moment $= F \times d_\perp$;
equilibrium: $\sum F = 0$, $\sum M = 0$
- ☐☐☐ Projectiles (speed U , angle α):
 $x = Ut \cos \alpha$, $y = Ut \sin \alpha - \frac{1}{2}gt^2$
- ☐☐☐ Slope at θ : weight component $mg \sin \theta$ down the slope; $R = mg \cos \theta$ if nothing else acts perpendicular to it
- ☐☐☐ Speed $= |\mathbf{v}|$; velocity-time graph: gradient = acceleration, area = displacement

Statistics & probability

- ☐☐☐ Mean: $\bar{x} = \frac{\sum x}{n} = \frac{\sum fx}{\sum f}$
- ☐☐☐ Standard deviation:
 $\sigma = \sqrt{\frac{\sum xx}{n} - \bar{x}^2} = \sqrt{\frac{\sum x^2}{n} - \bar{x}^2}$
- ☐☐☐ Outliers (common rule):
 $< Q_1 - 1.5(Q_3 - Q_1)$ or
 $> Q_3 + 1.5(Q_3 - Q_1)$
- ☐☐☐ Coding $y = \frac{x-a}{b}$: $\bar{x} = a + b\bar{y}$,
 $\sigma_x = |b| \sigma_y$
- ☐☐☐ Union:
 $P(A \cup B) = P(A) + P(B) - P(A \cap B)$
- ☐☐☐ Intersection:
 $P(A \cap B) = P(A) \times P(B | A)$
- ☐☐☐ Conditional:
 $P(A | B) = \frac{P(A \cap B)}{P(B)}$
- ☐☐☐ Independent:
 $P(A \cap B) = P(A)P(B)$,
 $P(A | B) = P(A)$
- ☐☐☐ Binomial $X \sim B(n, p)$:
 $P(X = x) = \binom{n}{x} p^x (1 - p)^{n-x}$
- ☐☐☐ Binomial mean, variance:
 $E(X) = np$, $\operatorname{Var}(X) = np(1 - p)$
- ☐☐☐ Standard normal:
 $Z = \frac{X - \mu}{\sigma} \sim N(0, 1)$
- ☐☐☐ Normal: points of inflection at $\mu \pm \sigma$; about 68%, 95%, 99.7% within 1, 2, 3 s.d.
- ☐☐☐ Normal approx. to $B(n, p)$ (n large, p near $\frac{1}{2}$): $N(np, np(1 - p))$
- ☐☐☐ Use a continuity correction, e.g. $P(X \leq 4) \approx P(Y < 4.5)$
- ☐☐☐ Sample mean:
 $\bar{X} \sim N\left(\mu, \frac{\sigma}{\sqrt{n}}\right)$, $Z = \frac{\bar{X} - \mu}{\sigma/\sqrt{n}}$
- ☐☐☐ Tests: reject H_0 if p -value $< \alpha$;
two-tailed: $\alpha/2$ each tail; PMCC test
 $H_0: \rho = 0$